

## Repair cost optimization for maintenance of RC structure subjected to carbonation

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### ABSTRACT

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When concrete is exposed to high concentration of CO<sub>2</sub>, pH in pore water drops below 10.5 and this allows acceleration of corrosion initiation in concrete, so called carbonation. With increasing significance in durability and maintenance of RC (Reinforced Concrete) structures, maintenance planning based on probabilistic method has been adopted for estimation of repair cost. In the work, repair costs from conventional and probabilistic method are evaluated with increasing intended service life (ISL). The changing probabilistic parameters such as safety index and repairs frequency are evaluated considering extension of ISL and varying coefficient of variation (COV). The effects of ISL and the service life through repair (repair-service life) on repair cost are evaluated, and the two methods are attempted to actual underground structure exposed to carbonation for estimation of repair cost and frequency. Unlike the cost from conventional method, the cost from probabilistic method is plotted as continuous function and is evaluated to be effective to save the repair cost by simply optimizing ISL. Furthermore probabilistic method can consider the uncertainties of construction or repair quality through changing COV of ISL and repair-service life.

**Keywords:** carbonation; repair-service life; probabilistic and conventional method; maintenance; initial service life

## Introduction

The problems caused by carbonation in underground structures have been reported due to increasing CO<sub>2</sub> concentration from 1990's [1, 2]. Carbonation is a representative deterioration phenomenon, which can cause corrosion in embedded steel by lowering pH in pore water [2-4]. In many Concrete Design Specification and Guidelines, durability design and the related maintenance strategy against carbonation have been proposed [5, 6]. A deterministic method has been conventionally adopted for determination of service life and repairing timing. The method needs a quantitative methodology for carbonation process and the evaluated carbonation depth is designed not to exceed the design cover depth within (ISL intended service life) [2, 5, 6]. From 1950's the governing equation for carbonation has been studied with semi-empirical form [1]. From 1990's, they have been enhanced with considering concrete behaviors in early age such as pore structure development, moisture transport, and carbonic reactions [3, 4, 7-9]. In another method, so called probability-based method, design parameters like cover depth,



mix proportions, and environmental conditions are considered as random variables with probability distributions. The carbonation design based on probability method induces the condition that the probability of steel corrosion should be smaller than the maximum allowable probability within ISL. This technique has been enhanced and developed for evaluation of damaged area due to carbonation and remaining service life with spatial variability characteristics [10-12]. The concept of maintenance free period has been introduced from 1990's considering initial construction conditions and it is very important for determination of maintenance strategy and extension of service life through repairs. Recently the significance in LCCA (Life Cycle Cost Analysis) is increasing and probabilistic techniques are adopted. However they simply estimate total cost based on an optimization of each process without service life from engineering modeling based on carbonation process [13-16]. Among the previous works utilizing probability technique, reduction of repairing cost and CO<sub>2</sub> emission were attempted considering probability distributions of ISL and repair-service life [17, 18], however the effects of design parameter on service life and repairing frequency were not quantitatively evaluated.

In the work, two probabilistic distributions for initial and repair-service are considered, and design parameters for repair cost estimation such as safety index and repair frequency are evaluated. The effect of extension of initial and repair-service on repair feasibility and the related cost are also simulated. Utilizing the initial and repair cost from previous study, actual repair cost and the savings are obtained from the comparison of the results between conventional and probabilistic method for RC underground structure exposed to carbonation.

## Repairing Cost Evaluation with Probability Analysis for Carbonation

### Carbonation mechanism

Carbonation is determined as a deterioration phenomenon due to time effect. In the carbonic process, calcium hydroxide in cement hydration products reacts with carbon dioxide and turns into calcium carbonate, during which pH in pore water drops below 10.5 and the condition for corrosion initiation starts due to broken passive film around steel. The reaction of carbonation in concrete can be written as Eq. (1) and the schematic diagram is shown in Figure 1.

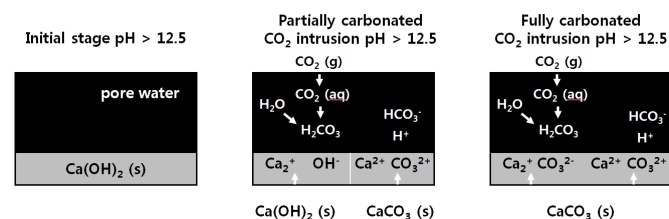
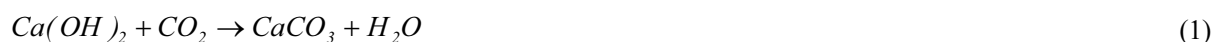


Figure 1. Carbonation reaction and changing material properties [21].

The properties in carbonated concrete are changed with carbonation progress. Porosity and saturation in carbonated concrete are altered by additional produced calcium carbonate and reduced surface tension in pore water [19, 20]. Many researches have been performed for an accurate carbonation modeling which can be capable of handling local environment condition, thermos-dynamic carbonation reaction, and interactions of various cations in cementitious materials [4, 9, 21].

### Background theory for probability analysis for determination of repairing timing

The probability-based evaluation for repairing time has been explained well in the previous works [17, 18]. In the section, the background theory is briefly summarized. Two probability distributions are assumed as normal distributions for initial and repair-service life that is extended service life through repair. The condition for without repair can be determined as Eq. (2), where  $T_1$  and  $T_{end}$  are the 1<sup>st</sup> repairing period and ISL, respectively.

$$T_1 \geq T_{end} \quad (2)$$

In the condition, PSLF (Probability of Service Life) can be calculated as Eq. (3).

$$P_1 = \int_{\beta_1}^{\infty} \frac{1}{\sqrt{2\pi}} \exp\left(-\frac{\beta^2}{2}\right) d\beta \quad (3)$$

where  $P_1$  is PSL which requires 1st repairing timing and  $\beta_1$  is safety factor (normalizing factor) consisting of time, mean of the 1st service life ( $\overline{T}_1$ ), and standard deviation of  $\overline{T}_1$ . the safety factor in the condition is given as Eq. (4).

$$\beta_1 = \frac{t_2 - (\overline{T}_1 + \overline{T}_2)}{\sqrt{\sigma_1^2 + \sigma_2^2}} \quad (4)$$

where  $\overline{T}_i$  and  $\sigma_i$  are mean and standard deviation of  $i^{th}$  repairing time with increasing  $t_2$  ( $T_1 + T_2$ ).

The condition for permitting only the 1st repairing time can be shown in Figure 2 considering the probability area of  $\overline{T}_i$ .

$P_2^*$  in Figure 2 can be calculated through Eq. (5) and PSLF of 1st repairing time can be written as Eq. (6)

$$P_2^* = 1 - \int_{-\infty}^{\beta_2} f(\beta) d\beta = \int_{\beta_2}^{\infty} f(\beta) d\beta = \int_{\beta_2}^{\infty} \frac{1}{\sqrt{2\pi}} \exp\left(-\frac{\beta^2}{2}\right) d\beta \quad (5)$$

$$P_2 = (1 - P_1) \times P_2^* \tag{6}$$

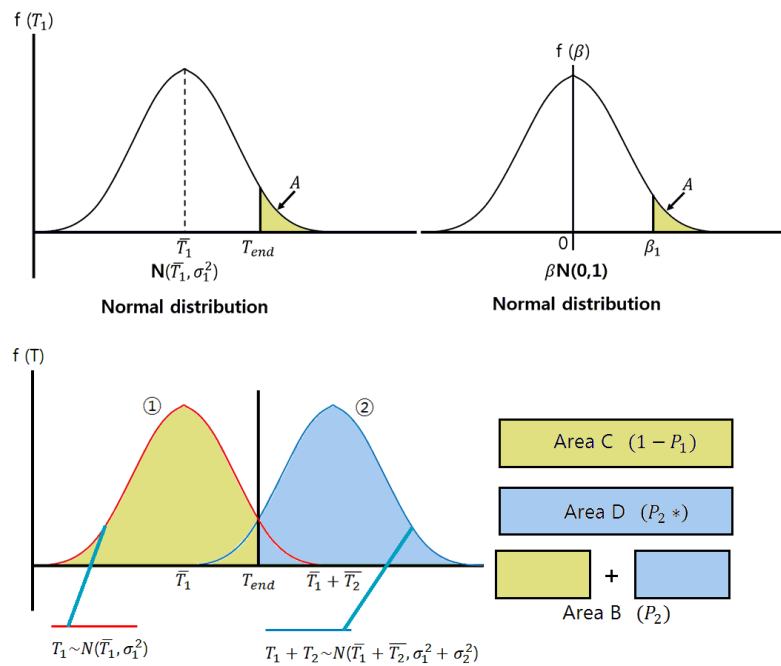


Figure 2. Concept of PSL for the 1st repairing timing [17].

With increasing number of repairing,  $P_n$  for  $n^{\text{th}}$  repairing time can be generalized as Eq. (7) and total repair cost ( $C_{total}$ ) in a given cost ( $C$ ) per repairing can be determined as Eq. (8).

$$P_n = (1 - \sum_{k=1}^{n-1} P_k) \times P_n^* \tag{7}$$

$$C_{total} = \sum_{k=1}^n (kCP_k) \tag{8}$$

## Repair Cost Simulation Approach for RC Structure under Carbonation

### Outline of simulation

In the section, a given condition is assumed and the effects of changing design parameters are investigated on the number of PSL and repair cost. In the field investigation, the initial service life which does not need repair (maintenance free period) is approximately 40~50 years in normal construction condition [22]. The initial service life and repair-service life are assumed as 40 and 20 years, respectively. The quality of construction is closely related with COV of service life, so that COVs for initial and repair-service life are assumed as 0.20 which seems to

be reasonable. The level of COV (0.15~0.20) is allowable construction variation for steel location, cover depth, and locally varied quality of concrete. The control case for analysis is listed in Table 1.

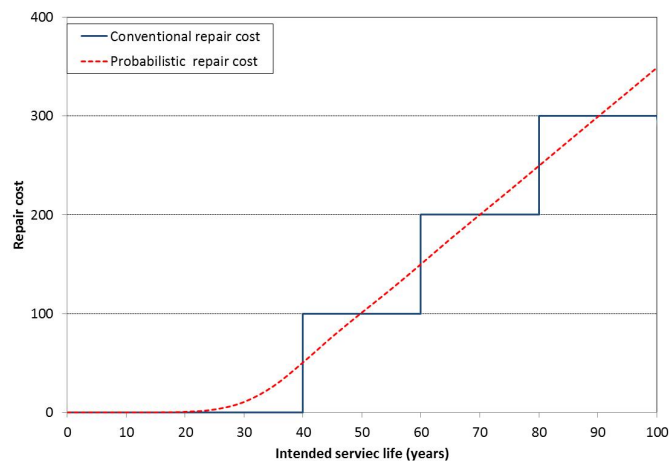
**Table 1.** Analysis case for repair cost with ISL

Initial service life	Repair-service life through 1 <sup>st</sup> repair	Cost for Initial Service life	Cost for each repair	COV
40	20	-	100	0.2 for initial service 0.2 for repair-service life

## Effects of design parameters on repair cost

### Simulation of control case

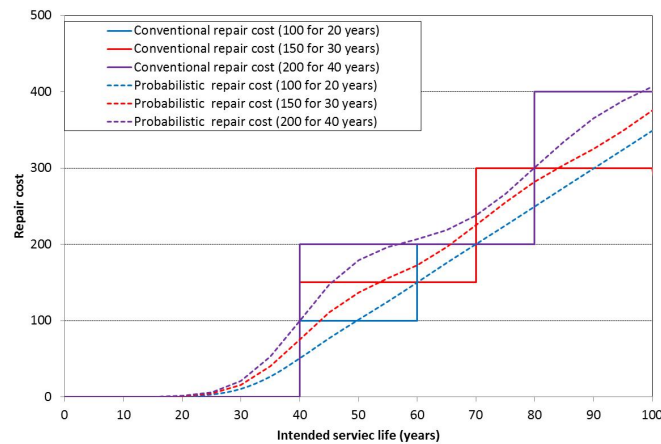
Control case for maintenance is simulated with increasing ISL. Control case includes 40 years of initial service life and 20 years of repair- service life. The results are shown in Figure 3 where the cost from probabilistic method shows a continuous line. After 100 years, the cost with repeated repairs is 300 for conventional method and 348.8 for probabilistic method. The cost from probability method is much higher than that from probabilistic method at 100 years, however the cost from probability shows more cost-benefit when ISL is shortened to 80~90 years. In the previous researches [17, 18], the cost function from probabilistic method always crosses the middle of cost jumping from conventional method since mean values in the both probabilistic distributions are considered at the period.



**Figure 3.** Repair cost with increasing ISL.

### Effect of repair-service life extension on repair cost

In the given initial service life, the repair cost from probabilistic method is compared with varying extension repair-service life. The cost for repair is assumed to linearly increase with extension of service life, which is 100 for 20 years, 150 for 30 years, and 200 for 40 years of extension. The results are shown in Figure 4.

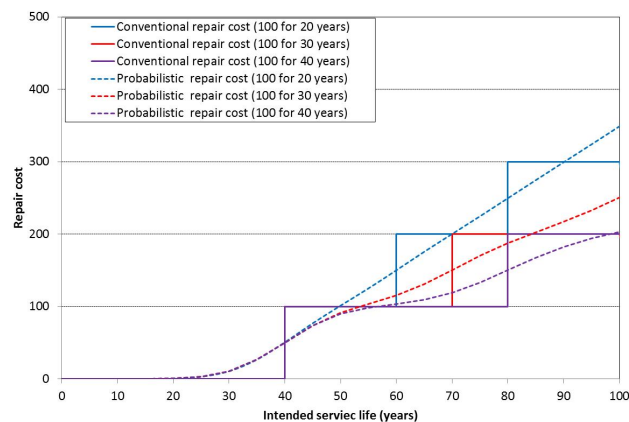


**Figure 4.** Repair cost estimation with increasing service life and cost of repair.

As shown in Figure 4, the final repair costs to 100 years are 300 (20 years of repair-service life), 300 (30 years of repair-service life), and 400 (40 years of repair-service life) for conventional method while the costs to each repair-service life are 348.8, 375.5, and 406.6 for probabilistic method, respectively. If the ISL is changed to 80 years, the least cost is 150 from conventional method, however minimum repair cost is evaluated to 274 from probabilistic method when ISL is assumed as 85 years. With varying ISL, the optimum cost changes. Before construction, maintenance planning with repair cost is important since, it determines of repair frequency and the related cost.

In the condition of constant repair cost with repair-service life, the cost in Figure 4 is changed to Figure 5.

As shown in Figure 5, the total cost can be reduced significantly with extension of repair-service life with constant repair cost. It means the extended service life due to repair with low cost is a key parameter in the maintenance planning. When ISL is determined as 100 years, the least cost is 200 from conventional method with 40 years of repair-service life. If ISL is assumed as 85 and 90 years, the least costs are 167.5 and 182.4 from probability method, respectively.



**Figure 5.** Repair cost estimation with increasing service life and constant cost of repair.

### Effect of additional service life and quality on repair cost

The pattern of repair cost varies with changing COV. With a given initial and repair-service life, COV for each service life is changed to from 0.2 to 1.0. The initial and repair-service life are assumed as 40 years and 20 years, respectively. The results are plotted in Figure 6.

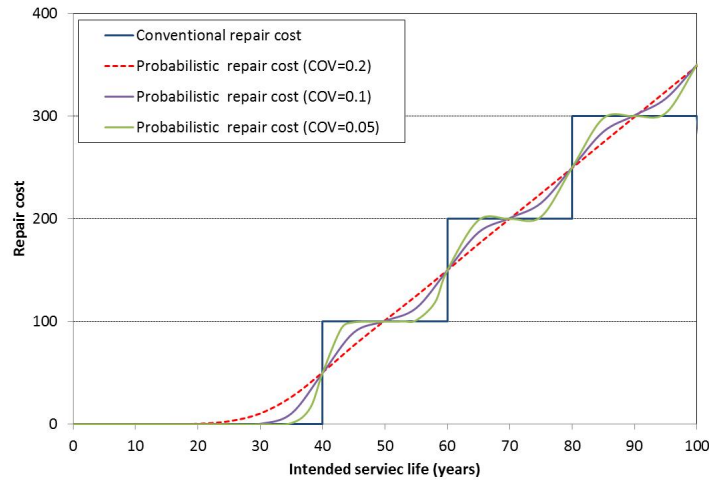


Figure 6. Effect of COV variation of each service life on repair cost.

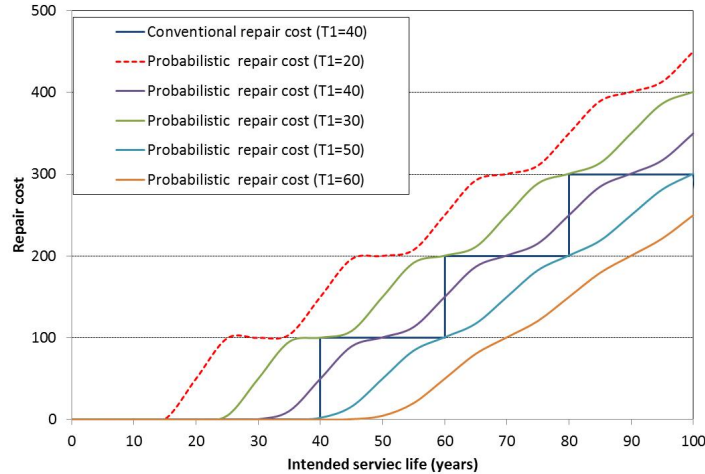


Figure 7. Cost repair with varying initial service life and constant repair-service life.

As shown in Figure 6, the results from probabilistic method approach to those from conventional method with decreasing COV. The COV of service life is much related with construction quality and the uncertainties in construction [11]. As shown in the results, the repair cost varies in spite of the same initial and repair-service life. For example, when ISL is determined as 75 years, the cost from probability changes from 224.6 (COV: 0.2) to 215.4 (COV: 0.1) and 202.1 (COV: 0.05) with decreasing COV, respectively. The reasonable determination of COV which can represent an actual repair quality is necessary for maintenance planning.

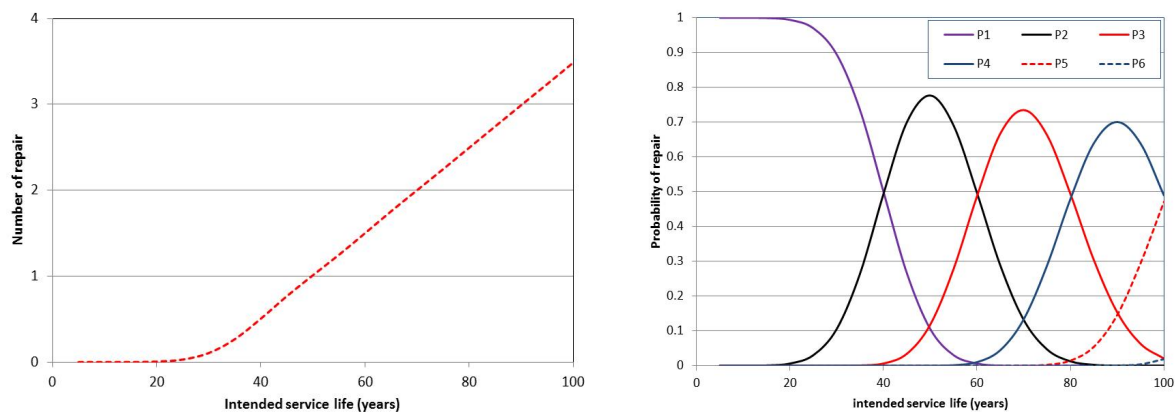
### Effect of initial service life and quality

In the section, the effect of extension of initial service life on repair cost is evaluated. For the analysis, initial service life assumed from 20 years to 60 year with fixed 20 years of repair-service and 0.1 of constant COV. The results are shown in Figure 7.

When ISL is determined as 100 years, the repair cost is 450 with 20 years of initial service life and it decreases by 50% with increasing initial service life to 60 years. The results can be expected easily since the results are almost same as those from conventional method.

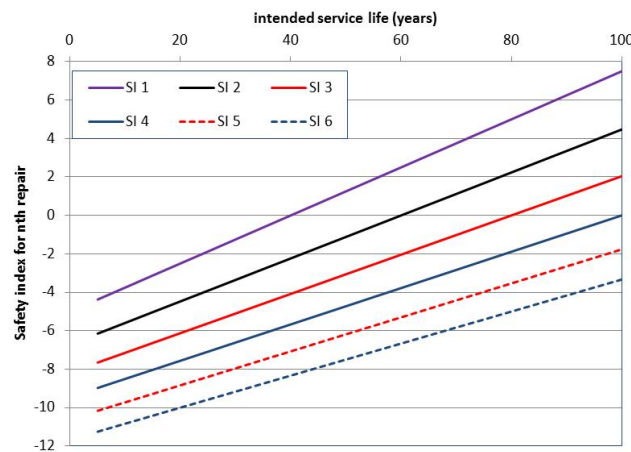
### Changes in probability parameters

With increasing ISL, the required number of repair also increases. In the given condition of 40 years of initial service life and 20 years of repair-service life, the required repair frequency increases as Figure 8(a), which shows 3.48 times of repairing at 100 years. During the period, the probability for repairing number is altered. Before 20 years, additional repair is not necessary since the initial service life with 0.2 of COV is dominant, however after 30



(a) Number of the required repairs with increasing ISL

(b) Probability of  $N^{\text{th}}$  repairing



(c) Probability of safety factor for  $N^{\text{th}}$  repairing

Figure 8. Changes in probability parameters with extension of ISL.



years, 1<sup>st</sup> repairing time comes so that probability for 1<sup>st</sup> repairing increases. With increasing ISL, probability  $P_i$  for  $i$ -1<sup>th</sup> repair event decreases but  $P_{i+1}$  for  $i$ <sup>th</sup> repair event increases. The changes in probability for  $i$ <sup>th</sup> repair are shown in Figure 8(b). The safety index in Figure 2, which means the starting point for calculation of failure probability increases with extension of ISL. The results of safety index are plotted in Figure 8(c).

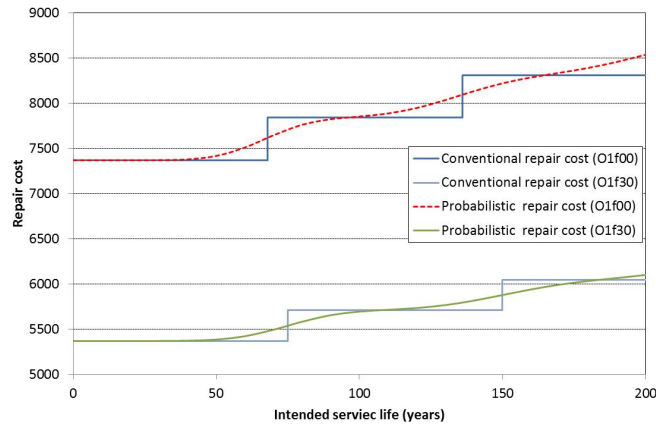
### Simulation of optimum repair cost based on actual carbonated concrete in underground RC structure

In the previous research [22, 23], 4 mix proportions were considered, and initial and repair-service life were obtained. 2 typical mix proportions were adopted and the result for each service life is summarized in Table 2. The calculation of total cost is shown in Figure 9.

**Table 2.** Initial and repair-service life for RC structure under carbonation from previous study [23]

Mix conditions	Initial service life and cost	Repair-service life and cost
O1F00	67 years and 7370	67 years and 470
O1F30	75 years and 5370	75 years and 339

- Exposure to 1200 ppm of CO<sub>2</sub>
- Total intended service life: 200 years
- Cover replacement technique and constant COV (0.2)



**Figure 9.** Total repair cost with increasing ISL.

As shown in Figure 9, total cost in O1f00 mix conditions shows 8,310 from the conventional method and 8,538 from probabilistic method, respectively. If the intended service life is optimized to 140 years, 8,134 from probabilistic method is much lower than shows 8,310 from conventional method, which shows 2.4% cost saving to initial construction cost by simply optimizing ISL. In the case of O1f30 mix conditions, 6,048 from conventional method and 6,101 from probabilistic method are evaluated. The ISL is optimized to 150 years, the gap from the methods is 169, which yields 3.2% cost saving to initial construction cost.

## Conclusions

In the work, the repair cost is evaluated from the probabilistic and conventional method, and the strong/weak point are compared as well. Adopting the previous research, total cost including initial construction cost is evaluated and quantitative cost-saving ratio is derived by simply optimizing ISL. The conclusions from the work are as follows.

1. The repair cost from probabilistic method is shown in the continuous line in contrast with conventional method. In the control case containing 40 years of initial service life and 20 years of repair-service life, 348.8 and 300 of repair cost are evaluated from probabilistic and conventional method at 100 years of ISL. If ISL is shortened to 80 years, 50 of repair cost is saved through adopting probabilistic method.
2. The repair- service life with low cost is a key parameter for repair cost optimization. When ISL is determined as 100 years, the least cost is 200 from conventional method with 40 years of repair-service life, however assuming 85 and 90 years of ISL, the optimized costs are 167.5 and 182.4 from probability method, respectively.
3. With decreasing COV of each service life, the result from probabilistic method turns into those from conventional method. The COV in service life is so closely related with construction and repair material quality that determination of reasonable COV for repairing technique is necessary.
4. Adopting the actual initial and repair cost for RC structure subjected to carbonation, 2.4~3.2% of cost saving to initial construction cost is evaluated from probabilistic method by optimization of ISL of the structure.

## Acknowledgement

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